

TRIGONOMETRY
PYQ'S
2025, 2024, 2023

2025

$\tan 2A = 3 \tan A$ is true, when the measure of $\angle A$ is:

1

- (a) 90° (b) 60°
(c) 45° (d) 30°

[2025]

Which of the following statements is true? [2025]

- (a) $\sin 20^\circ > \sin 70^\circ$ (b) $\sin 20^\circ > \cos 20^\circ$
(c) $\cos 20^\circ > \cos 70^\circ$ (d) $\tan 20^\circ > \tan 70^\circ$

Which of the following is a trigonometric identity? 1

- (a) $\sin^2 \theta = 1 + \cos^2 \theta$ (b) $\operatorname{cosec}^2 \theta + \cot^2 \theta = 1$
(c) $\sec^2 \theta = 1 + \tan^2 \theta$ (d) $\sin 2\theta = 2 \sin \theta$ [2025]

$\sec A = 2 \cos A$ is true for $A =$ [2025]

- (a) 0° (b) 30°
(c) 45° (d) 60°

If $x \left(\frac{2 \tan 30^\circ}{1 + \tan^2 30^\circ} \right) = y \left(\frac{2 \tan 30^\circ}{1 - \tan^2 30^\circ} \right)$, then $x : y =$

- (a) 1 : 1 (b) 1 : 2
(c) 2 : 1 (d) 4 : 1

[2025]

In a right triangle ABC, right-angled at A, if $\sin B = \frac{1}{4}$, then the value of $\sec B$ is [2025] 1

- | | |
|-----------------|---------------------------|
| (a) 4 | (b) $\frac{\sqrt{15}}{4}$ |
| (c) $\sqrt{15}$ | (d) $\frac{4}{\sqrt{15}}$ |
- (a) 4

(c) $\sqrt{15}$

If $x = \cos 30^\circ - \sin 30^\circ$ and $y = \tan 60^\circ - \cot 60^\circ$, then 1

- | | |
|-------------|---|
| (a) $x = y$ | (b) $x > y$ [2025] |
| (c) $x < y$ | (d) $x > 1, y < 1$ |

If $x = 2 \sin 60^\circ \cos 60^\circ$ and $y = \sin^2 30^\circ - \cos^2 30^\circ$ and $x^2 = ky^2$, the value of k is: 1

- | | |
|----------------|--|
| (a) $\sqrt{3}$ | (b) $-\sqrt{3}$ |
| (c) 3 | (d) -3 [2025] |

(A) Prove that $\frac{\cos A + \sin A - 1}{\cos A - \sin A + 1} = \operatorname{cosec} A - \cot A$ [2025]

(B) If $\cot \theta + \cos \theta = p$ and $\cot \theta - \cos \theta = q$,
prove that $p^2 - q^2 = 4\sqrt{pq}$ [2025]

(a) If $a \sec \theta + b \tan \theta = m$ and $b \sec \theta + a \tan \theta = n$,
prove that $a^2 + n^2 = b^2 + m^2$ [2025]

OR

(b) Use the identity: $\sin^2 A + \cos^2 A = 1$ to prove
 $\tan^2 A + 1 = \sec^2 A$. Hence, find the value of $\tan A$
when $\sec A = \frac{5}{3}$, where A is an acute angle.

(a) Prove that: $\frac{\cos \theta - 2\cos^3 \theta}{\sin \theta - 2\sin^3 \theta} + \cot \theta = 0$. [2025]

OR

(b) Given that $\sin \theta + \cos \theta = x$, prove that $\sin^4 \theta + \cos^4 \theta$
 $= \frac{2 - (x^2 - 1)^2}{2}$. [2025]

2024

If $\sec \theta - \tan \theta = m$, then the value of $\sec \theta + \tan \theta$ is:

(a) $1 - \frac{1}{m}$

(b) $m^2 - 1$

[2024]

(c) $\frac{1}{m}$

(d) $-m$

If $\cos(\alpha + \beta) = 0$, then value of $\cos\left(\frac{\alpha + \beta}{2}\right)$ is equal to:

(a) $\frac{1}{\sqrt{2}}$

(b) $\frac{1}{2}$

[2024]

(c) 0

(d) $\sqrt{2}$

A solid sphere is cut into two hemispheres. The ratio of the surface areas of sphere to that of two hemispheres taken together, is:

(a) 1 : 1

(b) 1 : 4

[2024]

(c) 2 : 3

(d) 3 : 2

The distance between the points $(a \cos \theta, -a \sin \theta)$ and $(a \sin \theta, a \cos \theta)$ is

(a) a

(b) $a\sqrt{2}$

[2024]

(c) 0

(d) $2a$

If $\sin A = \frac{2}{3}$, then value of $\cot A$ is: [2024]

(a) $\frac{\sqrt{5}}{2}$

(b) $\frac{3}{2}$

(c) $\frac{5}{4}$

(d) $\frac{2}{3}$

For $\theta = 30^\circ$, the value of $(2 \sin \theta \cos \theta)$ is:

(a) 1 (b) $\frac{\sqrt{3}}{2}$ [2024]

(c) $\frac{\sqrt{3}}{4}$ (d) $\frac{3}{2}$

. If $\sin \theta = \cos \theta$, ($0^\circ < \theta < 90^\circ$), then value of $(\sec \theta \cdot \sin \theta)$ is:

(a) $\frac{1}{\sqrt{2}}$ (b) $\sqrt{2}$ [2024]

(c) 1 (d) 0

. If $\sin \theta = \cos \theta$, ($0^\circ < \theta < 90^\circ$), then value of $(\sec \theta \cdot \sin \theta)$ is: [2024]

(a) $\frac{1}{\sqrt{2}}$

(b) $\sqrt{2}$

(c) 1

(d) 0

Assertion (A): If $\sin A = \frac{1}{3}$ ($0^\circ < A < 90^\circ$), then the value of $\cos A$ is $\frac{2\sqrt{2}}{3}$ [2024]

Reason (R): For every angle θ , $\sin^2 \theta + \cos^2 \theta = 1$.

The distance between the points $(a \cos \theta, -a \sin \theta)$ and $(a \sin \theta, a \cos \theta)$ is

(a) a

(b) $a\sqrt{2}$

[2024]

(c) 0

(d) $2a$

(a) Evaluate : $2\sqrt{2} \cos 45^\circ \sin 30^\circ + 2\sqrt{3} \cos 30^\circ$

OR

[2024]

(b) If $A = 60^\circ$ and $B = 30^\circ$, verify that: $\sin(A + B) = \sin A \cos B + \cos A \sin B$

Prove that : $\frac{\tan \theta}{1 - \cot \theta} + \frac{\cot \theta}{1 - \tan \theta} = 1 + \sec \theta \operatorname{cosec} \theta$

[2024]

(a) Evaluate : $2 \sin^2 30^\circ \sec 60^\circ + \tan^2 60^\circ$.

[2024]

OR

(b) If $2 \sin(A + B) = \sqrt{3}$ and $\cos(A - B) = 1$, then find the measures of angles A and B.

$0 \leq A, B, (A + B) \leq 90^\circ$.

Prove that $\frac{1 + \sec \theta - \tan \theta}{1 + \sec \theta + \tan \theta} = \frac{1 - \sin \theta}{\cos \theta}$. [2024]

Prove that $\sin^6 \theta + \cos^6 \theta = 1 - 3 \sin^2 \theta \cos^2 \theta$. [2024]

Prove that $\frac{\operatorname{cosec}^2 \theta - \sec^2 \theta}{\operatorname{cosec}^2 \theta + \sec^2 \theta} = \frac{3}{4}$, if $\tan \theta = \frac{1}{\sqrt{7}}$ [2024]

2023

Sec θ when expressed in terms of Cot θ , is equal to:

- (a) $\frac{1 + \cot^2 \theta}{\cot \theta}$ (b) $\sqrt{1 + \cot^2 \theta}$
(c) $\frac{\sqrt{1 + \cot^2 \theta}}{\cot \theta}$ (d) $\frac{\sqrt{1 - \cot^2 \theta}}{\cot \theta}$ [2023]

Which of the following is true for all values of θ ($0^\circ \leq \theta \leq 90^\circ$) ? [2023]

- (a) $\cos^2 \theta - \sin^2 \theta = 1$ (b) $\operatorname{cosec}^2 \theta - \sec^2 \theta = 1$
(c) $\sec^2 \theta - \tan^2 \theta = 1$ (d) $\cot^2 \theta - \tan^2 \theta = 1$

$(\sec^2 \theta - 1)(\operatorname{cosec}^2 \theta - 1)$ is equal to:

- (a) -1 (b) 1 [2023]
(c) 0 (d) 2

$\frac{\cos^2 \theta}{\sin^2 \theta} - \frac{1}{\sin^2 \theta}$, in simplified form is:

[2023]

- (a) $\tan^2 \theta$ (b) $\sec^2 \theta$
(c) 1 (d) -1

If θ is an acute angle of a right angled triangle, then which of the following equation is not true? [2023]

- (a) $\sin \theta \cot \theta = \cos \theta$ (b) $\cos \theta \tan \theta = \sin \theta$
(c) $\operatorname{cosec}^2 \theta - \cot^2 \theta = 1$ (d) $\tan^2 \theta - \sec^2 \theta = 1$

$(\cos^4 A - \sin^4 A)$ on simplification, gives [2023]

- (a) $2 \sin^2 A - 1$ (b) $2 \sin^2 A + 1$
(c) $2 \cos^2 A + 1$ (d) $2 \cos^2 A - 1$

If $\tan \theta = \frac{x}{y}$, then $\cos \theta$ is equal to [2023]

- (a) $\frac{x}{\sqrt{x^2 + y^2}}$ (b) $\frac{y}{\sqrt{x^2 + y^2}}$
(c) $\frac{x}{\sqrt{x^2 - y^2}}$ (d) $\frac{y}{\sqrt{x^2 - y^2}}$

(A) Evaluate: $\frac{5\cos^2 60^\circ + 4\sec^2 30^\circ - \tan^2 45^\circ}{\sin^2 30^\circ + \cos^2 30^\circ}$ [2023]

OR

- (B) If A and B are acute angles such that $\sin(A - B) = 0$ and $2\cos(A + B) - 1 = 0$, then find angles A and B.

(A) Prove that: $\frac{\sin A - 2\sin^3 A}{2\cos^3 A - \cos A} = \tan A$ [2023]

OR

- (B) Prove that $\sec A (1 - \sin A) (\sec A + \tan A) = 1$.

(A) Evaluate:

$$\frac{5}{\cot^2 30^\circ} + \frac{1}{\sin^2 60^\circ} - \cot^2 45^\circ + 2\sin^2 90^\circ$$
 [2023]

OR

- (B) If θ is an acute angle and $\sin \theta = \cos \theta$, find the value of $\tan^2 \theta + \cot^2 \theta - 2$.

(A) Evaluate $2\sec^2 \theta + 3 \operatorname{cosec}^2 \theta - 2\sin \theta \cos \theta$ if $\theta = 45^\circ$.

[2023]

OR

(B) If $\sin \theta - \cos \theta = 0$, then find the value of $\sin^4 \theta + \cos^4 \theta$. (B

If $\sin \theta + \cos \theta = p$ and $\sec \theta + \operatorname{cosec} \theta = q$, then prove that $q(p^2 - 1) = 2p$.

[2023]

Prove that: $\frac{1 + \sec A}{\sec A} = \frac{\sin^2 A}{1 - \cos A}$.

[2023]

Prove that $(\sin \theta + \cos \theta)(\tan \theta + \cot \theta) = \sec \theta + \operatorname{cosec} \theta$.

[2023]